

Q1.  $\int \sin x \sqrt{1 - \cos 2x} dx$  [ $\because$  Ans  $\frac{1}{\sqrt{2}} (x - \sin x \cos x) + C$ ]

Q2.  $\int \sqrt{1 + \sin \frac{x}{2}} dx$  [ $\because$  Ans  $4 \left[ \sin \frac{x}{4} - \cos \frac{x}{4} \right] + C$ ]

Q3.  $\int \frac{\sin^6 x + \cos^6 x}{\sin^2 x \cos^2 x} dx$  [ $\because$  Ans  $\tan x - \cot x - 3x$ ]

Q4.  $\int \frac{x^4}{1+x^2} dx$  [ $\because$   $\frac{x^3}{3} - x + \tan^{-1} x + C$ ]

Q5.  $\int \frac{\sin^2(\log x)}{x} dx$  [ $\because$   $\frac{1}{2} \left[ \log x - \frac{1}{2} \sin(2 \log x) \right]$ ]

Q6.  $\int \frac{\sec^4 x}{\sqrt{\tan x}} dx$  [ $\because$   $2 \left[ \sqrt{\tan x} + \frac{1}{5} (\tan x)^{5/2} + C \right]$ ]

Q7.  $\int \frac{dx}{x \sqrt{x^6 - 1}}$  [ $\because$   $\frac{1}{3} \sec^{-1} x^3 + C$ ]

Q8.  $\int \frac{1}{1 + \cot x} dx$  [ $\because$   $\frac{x}{2} - \frac{1}{2} \log(\sin x + \cos x)$ ]

Q9.  $\int \frac{\sqrt{\tan x}}{\sin x \cos x} dx$  [ $\because$   $2\sqrt{\tan x} + C$ ]

Q10.  $\int \frac{e^x + e^{-x}}{e^x - e^{-x}} dx$  [ $\because$   $\log |e^x - e^{-x}| + C$ ]

Q11.  $\int \frac{2 \sin \theta \cos \theta}{\sin^4 \theta + \cos^4 \theta} d\theta$  [ $\because$   $\tan^{-1}(\tan^2 \theta) + C$ ]

Q12.  $\int \tan x \tan 2x \tan 3x dx$  [ $\because$   $\frac{1}{3} \log |\sec 3x| - \frac{1}{2} \log |\sec 2x| - \log |\sec x| + C$ ]

Q13.  $\int \frac{dx}{\sqrt{1 + \sin x}}$  [ $\because$   $\sqrt{2} \log \left| \tan \left( \frac{\pi}{8} + \frac{x}{4} \right) \right| + C$ ]

$$\underline{\underline{Q14.}} \int \tan^3 x dx \quad [ \because \frac{1}{2} \tan^2 x - \log |\sec x| + c ]$$

$$\underline{\underline{Q15.}} \int \frac{dx}{\sin x \cos^3 x} \quad [ \because \frac{1}{2} \tan^2 x + \log_e |\tan x| + c ]$$

$$\underline{\underline{Q16.}} \int x^2 \sin^{-1} x dx \quad [ \because \frac{1}{3} x^3 \sin^{-1} x + \frac{1}{3} \sqrt{1-x^2} - \frac{1}{9} (1-x^2)^{3/2} + c ]$$

$$\underline{\underline{Q17.}} \int \log(x + \sqrt{a^2 + x^2}) dx \quad [ \because x \log(x + \sqrt{a^2 + x^2}) - \sqrt{a^2 + x^2} ]$$

$$\underline{\underline{Q18.}} \int \frac{x \sin^{-1} x dx}{\sqrt{1-x^2}} \quad [ \because -\sqrt{1-x^2} \sin^{-1} x + x + c ]$$

$$\underline{\underline{Q19.}} \int \frac{x}{1+\cos x} dx \quad [ \because \frac{x(1-\cos x)}{(1+\cos x)(1-\cos x)} \quad \text{Hint} \quad \underline{\underline{Ans}} = x(\cot x + \log \sin x + \csc x - \log \tan(\frac{x}{2})) + c ]$$

$$\underline{\underline{Q20.}} \int \sin \sqrt{x} dx \quad [ \because 2 [-\sqrt{x} \cos \sqrt{x} + \sin \sqrt{x}] + c ]$$

$$\underline{\underline{Q21.}} \int \frac{\log(\sec^{-1} x) dx}{x \sqrt{x^2-1}} \quad [ \because \sec^{-1} x [\log(\sec^{-1} x) - 1] + c ]$$

$$\underline{\underline{Q22.}} \int x^2 e^{x^3} \cos x^3 dx \quad [ \because \frac{1}{6} e^{x^3} (\sin x^3 + \cos x^3) + c ]$$

$$\underline{\underline{Q23.}} \int e^x (\cot x - \operatorname{cosec}^2 x) dx \quad [ \because e^x (\cot x + c) ]$$

$$\underline{\underline{Q24.}} \int e^x \left( \frac{1+\sin x}{1+\cos x} \right) dx \quad [ \because e^x \tan \frac{x}{2} + c ]$$

$$\underline{\underline{Q25.}} \int \frac{x + \sin x}{1+\cos x} dx \quad [ \because x \tan \frac{x}{2} + c ]$$

$$\underline{\underline{Q26.}} \int \frac{x^2+1}{x^2-1} dx \quad [ \because x + \log \left| \frac{x-1}{x+1} \right| + c ]$$

$$\underline{\underline{Q27.}} \int \frac{d\theta}{\sin^4 \theta + \cos^4 \theta} \quad [ \because \frac{1}{\sqrt{2}} \tan^{-1} \left[ \frac{\tan^2 \theta - 1}{\sqrt{2} \tan \theta} \right] ]$$